Selective Applicative Functors

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Motivating example • "read a string, if it is 'ping' then print 'pong', otherwise do nothing"

pingPongM :: IO () pingPongM = getLine >>= \s -> if s == "ping" then putStrLn "pong" else pure ()

What if we want to analyse it?

pingPongM :: IO () pingPongM = getLine >>= \s ->

 Sometimes it's useful to be able to ask "what are all the effects this computation might have?"

- We could use this to
 - pre-allocate resources
 - speculate execution, parallelism
 - (examples coming later)

if s == "ping" then putStrLn "pong" else pure ()

But we cannot do that here!

pingPongM :: IO ()
pingPongM =
 getLine >>= (s)->
 if s == "ping" then putS

Only known at *runtime*

if s == "ping" then putStrLn "pong" else pure ()

In general, Monad makes this impossible

class Monad f where
 return :: a -> f a
 (>>=) :: f a -> (a -> f b) -> f b

We cannot know a until we have peformed f a
So we cannot analyse the computation to find all its (potential) effects, we can only run it.



But let's take a simpler example

first execute this...

whenM :: Monad m => m Bool -> m () -> m ()

But let's take a simpler example

first execute this...

whenM :: Monad m => m Bool -> m () -> m ()

if it returned True, execute this, otherwise don't

Rewrite our example using when M

We will need fmap:

class Functor f where fmap :: (a -> b) -> f a -> f b

Now, to get IO Bool:

fmap (== "ping") getLine :: IO Bool

whenM :: Monad m => m Bool -> m () -> m ()



Rewrite our example using when M

pingPongM :: IO () pingPongM = getLine >>= \s ->

pingPongM :: IO () pingPongM = whenM (fmap (== "ping") getLine) (putStrLn "pong")

when M:: Monad m = > m Bool - > m () - > m ()

if s == "ping" then putStrLn "pong" else pure ()

But why is this better? Look at the definition of when M:



whenM :: Monad m => m Bool -> m () -> m () whenM x y = x >>= $b \rightarrow if b then y else return ()$

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Still a *runtime* value, but it only has two possible values

• We have some hope of statically analysing this code, because we can enumerate all the possibilities for b



whenM :: Monad m => m Bool -> m () -> m () whenM x y = x >>= $\langle b \rangle$ -> if b then y else return ()

But why is this better? Look at the definition of when M:

Still a *runtime* value, but it only has two possible values

• We have some hope of statically analysing this code, because we can enumerate all the possibilities for b • But we can't do it in this form, using >>=



whenM :: Monad m => m Bool -> m () -> m () whenM x y = x >>= $\langle b \rangle$ -> if b then y else return ()

But wait...

 Don't we already have an abstraction that... o is weaker than Monad o admits static analysis

Applicative Functors: 2007, Nottingham/London

FUNCTIONAL PEARL

Idioms: applicative programming with effects

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Abstract

In this paper, we introduce ldioms—an abstract characterisation of an applicative style of effectful programming, weaker than Monads and hence more widespread. Indeed, it is the ubiquity of this programming pattern which drew us to the abstraction. We shall take the same course in this paper, introducing the applicative pattern by diverse examples, then abstracting it to define the ldiom type class and associated laws. We compare this abstraction with monoids, monads and arrows, and identify the categorical structure of idioms.

Applicative Functors

class Applicative f where pure :: a -> f a (<*>) :: f (a -> b) -> f a -> f b

We can execute computations $f(a \rightarrow b)$ and fa in parallel (if we like).

V All effects are statically visible and can be examined before execution.

X Computations must be independent, hence no conditional execution.



Applicative functors	???	Monads





	Applicative functors	???	Monads	
h - y f (a h)				





	Applicative functors	???	Monads
			X
a	a -> Maybe a a -> [f ()]		







Applicative functors	???	Monads

pingPongM = whenM (fmap (=="ping") getLine) (putStrLn "pong")





Applicative functors	???	Monads





Applicative functors	Selective functors	Monads
		X
		X





Applicative functors	Selective functors	Monads



Selective Applicative Functors Goal: an abstraction that allows o static analysis, parallelism, speculative execution conditional effects

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class Applicative f => Selective f where select :: f (Either a b) -> f (a -> b) -> f b

The first computation is used to select what happens next: • Left a: you must execute the second computation to produce a b; • Right b: you may skip the second computation and return the b.

Selective Applicative Functors

class Applicative f => Selective f where select :: f (Either a b) -> f (a -> b) -> f b



V All effects are statically visible and can be examined before execution.



V We can speculatively execute both computations in parallel (if we

V A limited form of dependence, sufficient for conditional execution.

Why this particular formulation?

class Applicative f => Selective f where select :: f (Either a b) -> f (a -> b) -> f b

Parametricity tell us what select can do whenM can be implemented wrongly (unlessM)

But we love operators, so

(<*?) :: Selective f => f (Either a b) -> f (a -> b) -> f b $(<^{*}?) = select$

Example

pingPongS :: IO () pingPongS = whenS (fmap (=="ping") getLine) (putStrLn "pong") whenS :: Selective f => f Bool -> f () -> f () whenS x y = selector $<^*$? effect where selector :: f (Either () ()) selector = bool (Right ()) (Left ()) <\$> x

effect :: f (() -> ()) effect = const <\$> y

Define branch in terms of select...

branch :: Selective f => f (Either a b) -> f (a -> c) -> f (b -> c) -> f c

select :: Selective f => f (Either p q) -> f (p -> q) -> f q



Define branch in terms of select... select :: Selective f => f (Either p q) -> f (p -> q) -> f q branch x l r = fmap (fmap Left) x <*? fmap (fmap Right) l <*? r



More combinators

ifS :: Selective f => f Bool -> f a -> f a -> f a (< >) :: Selective f => f Bool -> f Bool -> f Bool |a < || > b = ifS a (pure True) b(<&&>) :: Selective f => f Bool -> f Bool -> f Bool a <&&> b = ifS a b (pure False) anyS :: Selective f => (a -> f Bool) -> [a] -> f Bool anyS $p = foldr ((\langle | \rangle) \cdot p) (pure False)$ allS :: Selective f => (a -> f Bool) -> [a] -> f Bool alls p = foldr ((<&&>) . p) (pure True)



- ifS x t e = branch (bool (Right ()) (Left ()) <\$> x) (const <\$> t) (const <\$> e)



Every Monad is Selective

selectM :: Monad m => m (Either a b) -> m (a -> b) -> m b selectM x y = x >>= $\langle e - \rangle$ case e of Left a -> (\$a) <\$> y Right b -> return b

Every Monad is Selective

selectM :: Monad m => m (Either a b) -> m (a -> b) -> m b selectM x y = x >>= e ->case e of Left a -> (\$a) <\$> y Right b -> return b

In fact, select = selectM is the definition of the semantics of select for a Monad. (rather like <*> = ap defines the semantics of Applicative for a Monad)

Every Monad is Selective

selectM :: Monad m => m (Either a b) -> m (a -> b) -> m b selectM x y = x >>= e ->case e of Left a -> (\$a) <\$> y Right b -> return b

 Some Monads may choose to implement select more efficiently \circ e.g. Haxl uses parallelism for $\langle * \rangle$, speculation for select

Every Applicative is Selective

selectA x y = (\e f -> either f id e) < x < y

• This is a valid implementation of select, o but may not be the only one. • Summary: \circ select = selectM \rightarrow conditional effects \circ select = selectA \rightarrow unconditional effects

selectA :: Applicative f => f (Either a b) -> f (a -> b) -> f b

Always executes y

Data validation example

data Validation e a = Failure e | Success a

The idea is that we can traverse a structure and report multiple errors

instance Semigroup e => Applicative (Validation e) where pure = Success Failure e1 <*> Failure e2 = Failure (e1 <> e2) Failure e1 <*> Success _ = Failure e1 Success <*> Failure e2 = Failure e2 Success f <*> Success a = Success (f a)

Data validation example

data Validation e a = Failure e | Success a

instance Semigroup e => Selective (Validation e) where select (Success (Right b)) _ = Success b select (Success (Left a)) f = (\$a) <\$> f select (Failure e) = Failure e

Accumulates errors in both computations

Data validation example

data Validation e a = Failure e | Success a

instance Semigroup e => Selective (Validation e) where select (Success (Right b)) _ = Success b select (Success (Left a)) f = (\$a) <\$> f select (Failure e) _ = Failure e

 Neither selectA nor selectM Cannot be a Monad!

Discard errors on the right if the condition failed

mkAddress

- :: Selective f
- => f Street
- -> f City
- -> f PostCode
- -> f Country
- -> f Address

mkAddress street city postcode country = Address <\$> street <*> city <*> ifS (hasPostCode <\$> country) (Just <\$> postcode) (pure Nothing) <*> country



Non-laws: \circ pure (Right x) <*? y == pure x o pure (Left x) <*? y == (\$x) <\$> y these would rule out over-approximation and under-approximation of effects

There are identity, distributive and associative laws

- But: Monads must satisfy select = selectM

Selective and Hax

What is Hax!?

- Solves the following problem: I want to write code that works with remote data

 - I want data-fetching to happen in parallel where possible o automatically, without me having to do anything
- In use at scale at Facebook for writing anti-abuse code

In HaxI: Applicative = parallel Monad = sequential e.g. mapM fetch things will fetch things in parallel

Conditionals

• We found short-cutting "and" and "or" useful:

(.), (.&&) :: Haxl Bool -> Haxl Bool -> Haxl Bool a . & b = dox <- a if x then b else return False

Particularly in cases like if simpleCondition .&& complexCondition then .. else ..



But sometimes it's not easy to know the best ordering

• ... especially when the number of conditions is large,

if either condition returns False early, we don't need

Parallel boolean operators

pAnd, pOr :: Haxl Bool -> Haxl Bool -> Haxl Bool

• These are semantically the same as (.&&), (.||) o but evaluate both arguments in parallel o and bail out early if the answer is known

• But if we define

instance Selective Haxl where select = ...



pAnd = (<&&>)por = (<||>)

speculative/parallel.



And the rest of the selective combinators will now be

But there's a subtle problem...

- select will always execute its first argument to completion
- whereas we want pAnd to abort the first argument if the second argument returns False
 - o e.g. (someFetch >>= x) `pAnd` return False
 - should never execute x

Select is not precisely what we want But we can define a symmetric alternative:

biselect

- :: Selective f
- => f (Either a b)
- -> f (Either a c)
- -> f (Either a (b,c))

Solution: Add biselect as a method in Selective Instances can override biselect if they want



Generalisation

We have:

ifS :: Selective f => f Bool -> f a -> f a -> f a

Alternatively: bindBool :: Selective f => f Bool -> (Bool -> f a) -> f a



Generalisation We have:

ifS :: Selective f => f Bool -> f a -> f a -> f a

Alternatively:

bindBool :: Selective f => f Bool -> (Bool -> f a) -> f a

Moreover:

bindS :: (Selective f, Bounded a, Enum a, Eq a) => f a -> (a -> f b) -> f b

Look familiar?





bindS

- :: (Selective f, Bounded a, Enum a, Eq a) => f a -> (a -> f b) -> f b
- Implementation in terms of select could sequentially check all the possible values of a • But for a monad, bindS = (>>=)suggests that bindS should be a method



More applications • Build systems: extract all build dependencies before execution, with conditional execution Modelling processor instructions:

- access)
- Parsing combinators: Use Selective instead of Alternative to avoid backtracking



 Categorising instructions: Functor (e.g. increment), Applicative (arithmetic), Selective (branching), Monad (indirect memory

Conclusions

Selective identifies a useful point in the design space between Applicative and Monad
Combines the benefits of Applicative (static analysis, parallelism, speculation) with limited conditional support

Example: a blog engine

getPostIds :: Haxl [PostId] getPostContent :: PostId -> Haxl PostContent

I want to fetch all the content of all the posts:

getAllPostsContent :: Haxl [PostContent] getAllPostsContent = getPostIds >>= mapM getPostContent

 Just use standard monadic combinators mapM getPostContent should happen in parallel

Batching

• • •

Indeed, not just parallel, but batching multiple requests where possible:

Unbatched

SELECT content FROM posts WHERE postid = id1

SELECT content FROM posts WHERE postid = id2

Batched

SELECT content FROM posts WHERE postid IN {id1, id2, ...}

data Result a = Done a Blocked (Seq BlockedRequest) (Haxl a)

newtype Haxl a = Haxl { unHaxl :: IO (Result a) }

This is the result of a computation

Done indicates that we have finished

data Result a = Done a Blocked (Seq BlockedRequest) (Haxl a)

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data Result a = Done a Blocked (Seq BlockedRequest) (Haxl a)

newtype Haxl a = Haxl { unHaxl :: IO (Result a) }

Blocked indicates that the computation requires this data.

data Result a = Done a Blocked (Seq BlockedRequest) (Haxl a)

newtype Haxl a = Haxl { unHaxl :: IO (Result a) }

Haxl is in IO, because we use IORefs to store results



instance Monad Haxl where return a = Haxl \$ return (Done a) Haxl $m \rightarrow = k = Haxl $ do$ r <- m case r of Done a -> unHaxl (k a) Blocked br c -> return (Blocked br (c >>= k))

If m blocks with continuation c, the continuation for m >>= k is c >>= k

Haxl works by having a special Applicative instance

```
instance Applicative Haxl where
 pure = return
 Haxl f <*> Haxl x = Haxl $ do
   f' <- f
   x' <- x
   case (f',x') of
     (Done g, Done y ) -> return (Done (g y))
     (Done g, Blocked br c) -> return (Blocked br (g <$> c))
```

 when we use <*> we get parallelism when we use >>= we get sequentiality

- (Blocked br c, Done y) -> return (Blocked br (c <*> return y))
- (Blocked br1 c, Blocked br2 d) -> return (Blocked (br1 <> br2) (c <*> d))

Direct implementation

pAnd :: Haxl Bool -> Haxl Bool -> Haxl Bool pAnd (Haxl a) (Haxl b) = Haxl \$ do x <- a case x of Done False -> return False Done True -> b Blocked bx cx -> do y <- a case y of Done False -> return False Done True -> return x Blocked by cy -> Blocked (bx <> by) (cx `pAnd` cy)

• When we say this is "parallel", what do we mean? o data-fetches are done in parallel where possible NOT that we do the computation in parallel

o if both sides get blocked, we do their fetches together

Using Selective

instance Selective Haxl where select (Haxl x) (Haxl f) = Haxl \$ do rx < - xcase rx of Done (Right b) -> return (Done b) Blocked bx c -> do rf < -fcase rf of Blocked by d ->

Done (Left a) -> unHaxl ((\$a) <\$> Haxl f)

Done f -> unHaxl (either f id <\$> c) return (Blocked (bx <> by) (select c d))

Define branch in terms of select... select :: Selective f => f (Either p q) -> f (p -> q) -> f q branch x l r = select x l

Would make b == c



Define branch in terms of select... select :: Selective f => f (Either p q) -> f (p -> q) -> f q branch x l r = select (fmap (either Left (Right . Left)) x) $(fmap (\f -> Right . f) 1)$

- q = Either b c



Define branch in terms of select... select :: Selective f => f (Either p q) -> f (p -> q) -> f q q = Either b c $branch \times l r =$ select (select (fmap (either Left (Right . Left)) x) $(fmap (\langle f - \rangle Right . f) 1)$



Define branch in terms of select... select :: Selective f => f (Either p q) -> f (p -> q) -> f q branch x l r = select (select (fmap (either Left (Right . Left)) x) fmap (fmap Left) $(fmap (\f -> Right . f) 1)$



Define branch in terms of select... select :: Selective f => f (Either p q) -> f (p -> q) -> f q branch x l r = select (select (fmap (either Left (Right . Left)) x) fmap (fmap Left) (fmap (\f -> Right f) l) fmap (fmap Right)

